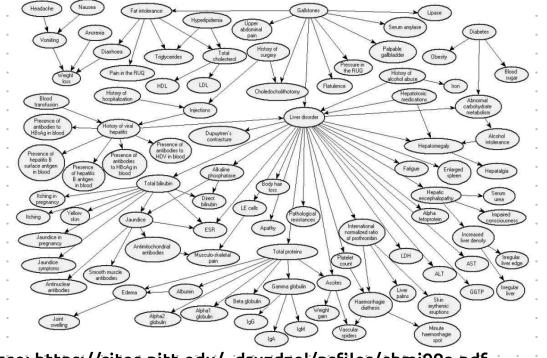
Đ:	S 2	25	00	-M	ar	24	1.

From last time (included for completeness today):

-P(ABC|XYZ) = P(ABCXYZ) / P(XYZ)- - - - - - - - computing conditional probabilities 

- compute conditional probabilities with multiple random variables:

WHAT ARE BMES NETS



source: https://sites.pitt.edu/~druzdzel/psfiles/cbmi99a.pdf

Bayes nets allow us to incorporate multiple pieces of evidence into some conditional prob of interest:

given a person has:

- symptom 4
- symptom 11
- risk factor 7

whats the prob of liver disorder?

Bayesian Network (Bayes Net)









(formally):

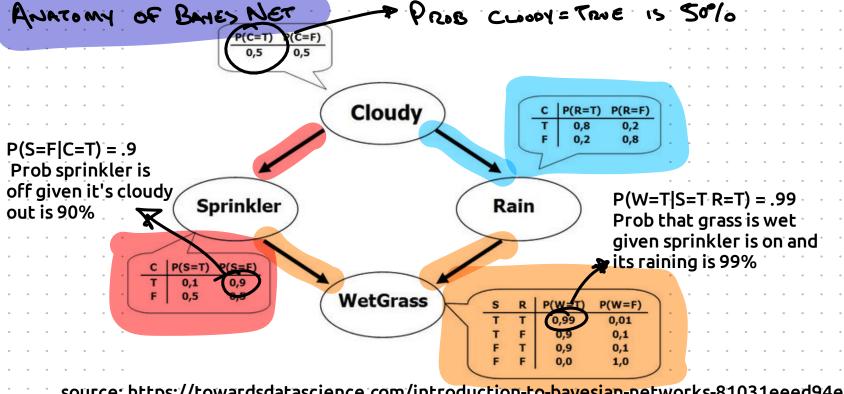
A directed, acyclic graph which represents conditional distributions / independences between a set of random variables. (B) HAS CYCLE, NOT

each node represents a random variable directed edges represent conditional distributions any node without inward edges has prob specified (its part of "bayes net" too!)

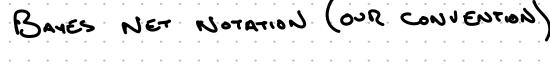


(informally):

a network which describes how random variables influence each other, can be used to compute conditional probabilities of interest

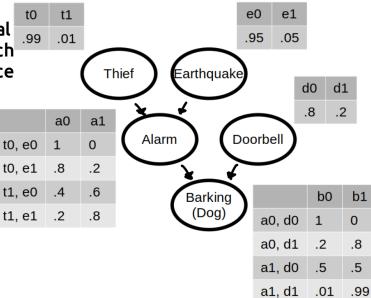


source: https://towardsdatascience.com/introduction-to-bayesian-networks-81031eeed94e



Each random variable is denoted with a capital letter (T for Thief). Each outcome in sample space has its own lowercase letter:

t0 = no thief
t1 = thief



(quick) ICA X: what's prob of earthquake?

given a thief in house, but no earthquake, what's prob alarm goes off?

interpretation question:
- is alarm better at detecting thieves or earthquakes?

- which sound bothers the dog more, the alarm or doorbell? In Class Assignment (last time): Estimate / intuite the four probabilities below. Is it greater / lesser / equal to other prob immediately above?

What is the prob of thief? 
$$Q(T=1)=1\%$$
  
Given that alarm is going off, what is prob of thief?

WHEN ALTON GOES OFF THON

### How do we compute conditional probabilities from a Bayes Net?

With a computer:

Step 1: Rewrite conditional probability without conditional

Step 2: In a spreadsheet, compute prob of every possible combination of outputs for all vars
Step 3: Compute the needed probabilities from step 1 via marginalization

P(a|b)P(b) = P(ab)

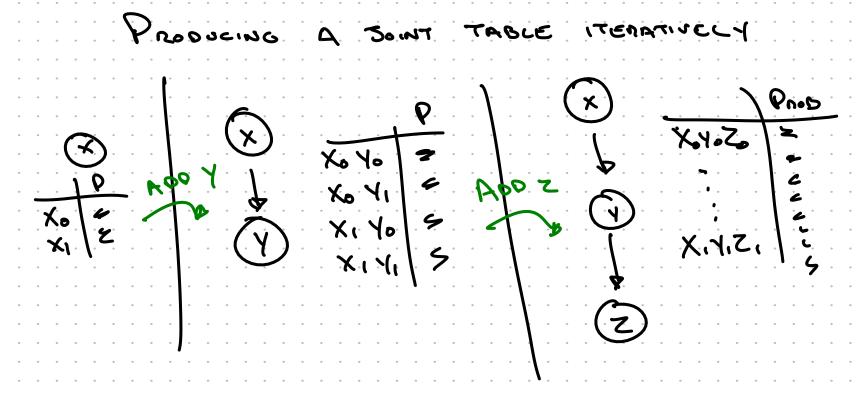
$$P(T|F=1) = P(F=1) P(T=1|F=1) = P(F=1) P(T=1|F=1) = P(F=1) P(T=1|F=1) = P(F=1) P(T=1|F=1) = P(F=1|F=1) = P(F$$

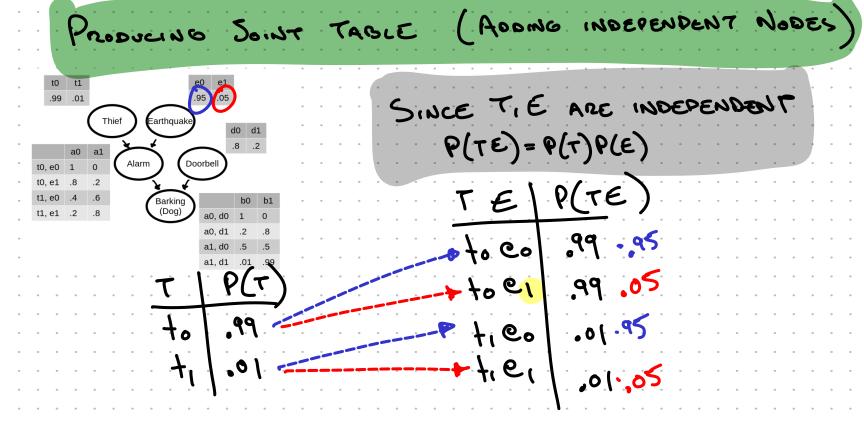
# Step 1: write conditional probabilities as ratio of (not conditional) probabilities

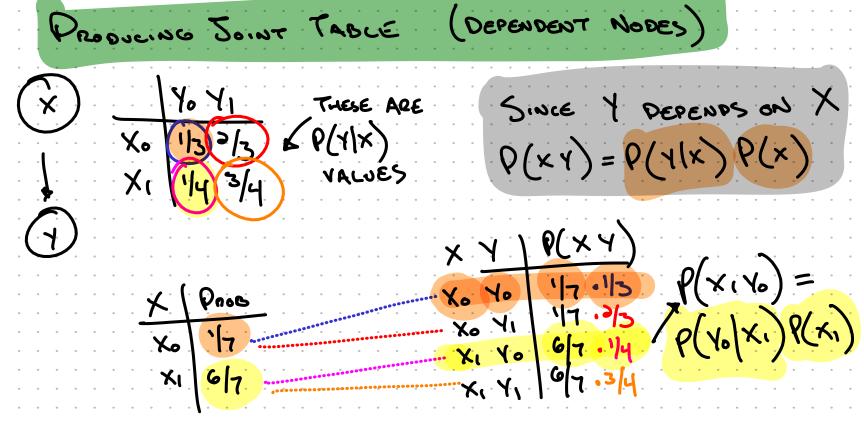
Step 2: In a spreadsheet, compute prob of every possible combination of outputs for all vars

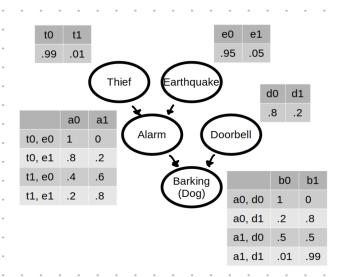
							D. Darking	D. DOUIDEII	A. Alailli	I. IIIIei	c. carinqu		(BUALE)
۰	٠	۰	٠	٠	۰	•	b0	d0	a0	tO	e0		0.7524
	۰	•	۰	٠	۰		b0	d0	a0	tO	e1		0.03168
	۰		-				b0	d0	a0	t1	e0		0.00304
	-11	50	4				b0	d0	a0	t1	e1		8E-05
E	7				Cie	در	b0	d0	a1	tO	e0		0
	٠		<b>6</b> 1	31	•	۰	b0	d0	a1	tO	e1		0.00396
-	ابر <sup>.</sup> س	>		٠	۰	۰	b0	d0	a1	t1	e0		0.00228
	•				۰	۰	b0	d0	a1	t1	e1		0.00016
	- •		L	7			b0	d1	a0	tO	e0		0.03762
	V	~					b0	d1	a0	tO	e1		0.001584
•	•	۰	•	•	•	۰	b0	d1	a0	t1	e0		0.000152
۰	٠	۰	٠	٠	۰	•	b0	d1	a0	t1	e1		4E-06
۰	٠	۰	٠		٠	•	b0	d1	a1	tO	e0		0
							b0	d1	a1	tO	e1		1.98E-05
							b0	d1	a1	t1	e0	N	1.14E-05
							b0	d1	a1	t1	e1		8E-07
۰	۰	۰	۰	۰	۰	۰	b1	d0	a0	tO	e0		0
۰	۰	۰	٠	•	٠	۰	b1	d0	a0	tO	e1		0

PROP









# In Class Exercise (don't submit):

Build the joint distribution table for the bayes net on the left.

(You needn't submit for credit. You can check your work with the given final answer csv on website)

MARCINALIZING IN SOINT TABLE (step 3)

COMPUTE P(XOZO) = P(X0Z0Y0) + P(X0Z0Y1) = 14 +0 = 14

MUSCINALIZING IN X Y Z / Pros SOINT TROLE 1 Yo Z. 14 QUICK PRACTICE Y. Y. Z. O COMPORE P(4, X,) = 041/4=1/4 Ko Y, Zo X0 Y Z1 1, 7, Zo COMPUTE P(XD) = 1/4+0+0+1/8 X, Y. Z, 10 X1 4, Z. X1 Y, Z1 14 P(XYZ)

## Putting it all together:

Step 1: Rewrite conditional probability without conditional

Step 2: In a spreadsheet, compute prob of every possible combination of outputs for all vars Step 3: Compute the needed probabilities from step 1 via marginalization

Example:

Given alarm is going off and dog is barking, what is the probability of a thief?

$$\rho(t, a, b) = \rho(t, a, b) = .38125$$

#### In Class Exercise 1:

Explicitly compute each of the following

1. What is the prob of thief? 
$$P(t_1) = 0$$

1. What is the prob of thief? 
$$P(t_1) = 0$$

2. Given that alarm is going off, what is prob of thief?  $P(t_1|Q_1) = .38135$ 

3. Given that alarm is going off & dog is barking, what is prob of thief?  $P(t_1|Q_1) = .38135$ 

4. iven that alarm is going off, dog is barking & earthquake, what is prob of thief? = .038

Answer each question below with one sentence (please avoid algebraic motivations and appeal to our intuition):

- Why is the prob of 2 greater than the prob of 1?
- Why is the prob of 3 equal to the prob of 2?
- Why is the prob of 4 less than the prob of 2?

$$\rho(t, |\alpha, b, e)$$

$$= \rho(t, a, b, e)$$

$$= .038$$

$$P(+,|\alpha_1) = \frac{P(\alpha_1+1)}{P(\alpha_1)} = .38125$$

Approach: compute the green and grey terms
above by summing prob of all rows which are
consistent

(i.e. green term is the sum of all rows where A=a1 and T=t1)

That spreadsheet work sure was cumbersome if only we could make the computer do all that busy	
work!	
In Class Assignment 2:	
Design the interface of a Bayes Net "library" which allows the user to	
Design the interface of a Bayes Net "library" which allows the user to	
1. specify a bayes net on discrete random variables (as shown here)	
as well as querying the bayes net for arbitrary:	
2. conditional distributions	
3. marginal distributions (i.e. not conditional distributions)	
This design is intentionally open-ended. You're welcome to write out notes on paper, though you can	

write function (or method) docstrings as well if you're ready.