

Admin

3/28 - Hw5 due 9pm

Lab 4-5 late deadline 9pm

lecture 3:25pm / zoom only

3/31 - review ex practice

4/4 - exam #2!

4/11 - second chance Hw 9pm

4/15 - project deadline!

Agenda

1. multiple linear regression

2. evaluation of MLR

3. Python

1. multiple linear regression

↳ supervised learning

- something we know
- something to ask  
--- training data w/known values

Simple Linear Regression

- need correlation first!
  - X, Y values (training)
  - predicts numeric values (targets)
- goal: classify based on features
- tweak by changing k
- euclidean for similarity

training / testing

X - independent var - features

Y - dep variable (target) - label

Logistic Regression

- binary classification
- probabilistic model
- slope varies

multiple linear regression

- ex - first linear regression

X - adm rate (ind.)

Y - tuition (dep) (target)

"real world" more than one X value influences Y

simple: one  $x$       multiple:  $x_1, x_2, x_3, \dots, x_n$   
one  $y$       one  $y$

$$y = mx + b \quad (\text{best fit}) \qquad y = m_1 \cdot x_1 + m_2 \cdot x_2 + \dots + m_n \cdot x_n + b$$

$m_1, m_2, \dots$  = regression coeffs  
 $x_1, x_2, \dots$  = ind. variables  
 $b$  = intercept

Python:

```
lr = LinearRegression()
lr.fit(x_train, y_train)
```

$\xrightarrow{\text{ind. variables}}$  targets } training data

lr.predict(x-test)

(ind. variables (testing data))

### Setting up data

→ start w/ data all together  
train-test-split to arbitrarily split

Hw5/Lab5 — random-state = 0

to draw ~ no random state, randomize  
train/test always same size,  
values randomly chosen

$y\text{-test}$  = actual targets  
compare to predicted targets

### 2. Evaluation of MLR

→ my supervised learning: compare actual vs. predicted

Ex: KNN / Logistic ~ accuracy, precision, recall, F1  
only have nominal data — were we wrong?

today: linear regression — all targets are numeric  
how wrong were we?

error

actual	predicted	error	
1.5	2	.5	$\text{MSE} = \frac{(1.5 - 2)^2 + (1.3 - 2)^2}{2}$
3.8	2.5	1.3	

How can we improve our model  
to get a better MSE? ~ no k

↳ clean up the data

- remove null values
- correct data types
- normalization
- remove outliers
- remove a feature or combine
- weight features



$$(.4)x + (.3)y + (.3)z$$