Homework 6: Turing Machines

CS 390 — Spring 2009

Assigned: March 23 Due: March 31 (Tuesday) 3:25

Problem 1 [30 points]

Give implementation-level description of Turing machines that decide the following languages over the input alphabet $\{0, 1\}$:

- 1. $\{w \mid w \text{ contains twice as many } 0 \text{ s as } 1 \text{ s} \}$
- 2. $\{w \mid w \text{ does not contain twice as many } 0 \text{ s as } 1 \text{ s} \}$

Problem 2 [20 points]

Exercise 3.9

Hint: For part (a), show that 2-PDAs can simulate Turing Machines, and for part (b), show that Turing Machines can simulate 3-PDAs.

Problem 3 [40 points]

Show that the collection of decidable languages is closed under the operation of:

- 1. Concatenation
- 2. Star
- 3. Complementation
- 4. Intersection

Problem 4 [10 points]

Exercise 3.6