# NLP \& Linguistics 

Natural Language Processing
CS 6120—Spring 2013
Northeastern University

David Smith<br>some slides from<br>Jason Eisner \& Chris Manning

## Engineering vs. Science?

- One story
- NLP took formal language theory and generative linguistics (same source?),
- Built small Al systems for a while,
- Then added statistics/machine learning.
- What now?
- Shouldn't Al tell us about natural intelligence?
- Are all NLP models lousy linguistics?


# Learning in the Limit Gold's Theorem 

## Observe some values of a function



## Guess the whole function



## Another guess: Just as good?



## More data needed to decide



## Poverty of the Stimulus

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- Never enough input data to completely determine the polynomial ...
- Always have infinitely many possibilities
... unless you know the order of the polynomial ahead of time.
- 2 points determine a line
- 3 points determine a quadratic
- etc.
- In language learning, is it enough to know that the target language is generated by a CFG?
" without knowing the size of the CFG?


## Language learning:

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Children listen to language [unsupervised]

## Language learning:

Children listen to language [unsupervised] Children are corrected?? [supervised]

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Remember: Language = set of strings

## Poverty of the Stimulus (1957)

Children listen to language
Children are corrected??
Children observe language in context
Children observe frequencies of language

## Poverty of the Stimulus (1957)

Chomsky: Just like polynomials: never enough data unless you know something in advance. So kids must be born knowing what to expect in language.

- Children listen to language
- Children are corrected??
- Children observe language in context
- Children observe frequencies of language


## Gold's Theorem (1967)

a simple negative result along these lines:
kids (or computers) can't learn much
without supervision, inborn knowledge, or statistics

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- Children observe language in context
- Children observe frequencies of language


## The Idealized Situation

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Mom talks

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- Mom talks
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- Guarantee: Any sentence of Mom's language is eventually uttered by Mom (even if infinitely many)


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- 1. Mom outputs a sentence
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- 3. Goto step 1
- Guarantee: Mom's language is in the set of hypotheses that Baby is choosing among
- Guarantee: Any sentence of Mom's language is eventually uttered by Mom (even if infinitely many)
- Assumption: Vocabulary (or alphabet) is finite.


## Can Baby learn under these conditions?

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- Learning in the limit:
- There is some point at which Baby's hypothesis is correct and never changes again. Baby has converged!
- Baby doesn't have to know that it's reached this point - it can keep an open mind about new evidence - but if its hypothesis is right, no such new evidence will ever come along.


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- Is there a perfect finite-state Baby?
- Is there a perfect context-free Baby?


## Languages vs. Grammars

Does Baby have to get the right grammar?
(E.g., does VP have to be called VP?)

Assumption: Finite vocabulary.

## Conservative Strategy

- Baby's hypothesis should always be smallest language consistent with the data
- Works for finite languages? Let's try it ...
- Language 1: \{aa,ab,ac\}
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Mom
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## Evil Mom

- To find out whether Baby is perfect, we have to see whether it gets 100\% even in the most adversarial conditions
- Assume Mom is trying to fool Baby
- although she must speak only sentences from L
- and she must eventually speak each such sentence
- Does Baby's strategy work?


## An Unlearnable Class

Class of languages:
= Let $L_{n}=$ set of all strings of length $<n$

- What is $\mathrm{L}_{0}$ ?
- What is $L_{1}$ ?
-What is $\mathrm{L}_{\infty}$ ?
- If the true language is $\mathrm{L}_{\infty}$, can Mom really follow rules?
-Must eventually speak every sentence of $\mathrm{L}_{\infty}$. Possible?
-Yes: $\varepsilon$; a, b; aa, ab, ba, bb; aaa, aab, aba, abb, baa, ...
- Our class is $C=\left\{L_{0}, L_{1}, \ldots L_{\infty}\right\}$


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- A perfect C-baby will distinguish among all of these depending on the input.
- But there is no perfect C-baby ...


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- Suppose Baby adopts conservative strategy, always picking smallest possible language in C.
- So if Mom's longest sentence so far has 75 words, baby's hypothesis is $L_{76}$.


## An Unlearnable Class

Our class is $C=\left\{L_{0}, L_{1}, \ldots L_{\infty}\right\}$

- Suppose Baby adopts conservative strategy, always picking smallest possible language in C.
- So if Mom's longest sentence so far has 75 words, baby's hypothesis is $L_{76}$.
- This won't always work: What language can't a conservative Baby learn?


## An Unlearnable Class

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Claim: Any perfect C-Baby must be "quasiconservative":
- If true language is $\mathrm{L}_{76}$, and baby posits something else, baby must still eventually come back and guess $\mathrm{L}_{76}$ (since it's perfect).


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- So if longest sentence so far is 75 words, and Mom keeps talking from $L_{76}$, then eventually baby must actually return to the conservative guess $\mathrm{L}_{76}$.


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- So if longest sentence so far is 75 words, and Mom keeps talking from $\mathrm{L}_{76}$, then eventually baby must actually return to the conservative guess $\mathrm{L}_{76}$.
- Agreed?


## Mom's Revenge

If longest sentence so far is 75 words, and Mom keeps talking from $L_{76}$, then eventually a perfect C-baby must actually return to the conservative guess $\mathrm{L}_{76}$.

- Suppose true language is $\mathrm{L}_{\infty}$.
- Evil Mom can prevent our supposedly perfect C-Baby from converging to it.
- If Baby ever guesses $\mathrm{L}_{\infty}$, say when the longest sentence is 75 words:
- Then Evil Mom keeps talking from $\mathrm{L}_{76}$ until Baby capitulates and revises her guess to $L_{76}$ - as any perfect C-Baby must.
- So Baby has not stayed at $\mathrm{L}_{\infty}$ as required.
- Then Mom can go ahead with longer sentences. If Baby ever guesses $L_{\infty}$ again, she plays the same trick again.


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- So Baby has not stayed at $\mathrm{L}_{\infty}$ as required.
- Conclusion: There's no perfect Baby that is guaranteed to converge to $L_{0}, L_{1}, \ldots$ or $L_{\infty}$ as appropriate. If it always succeeds on finite languages, Evil Mom can trick it on infinite language.


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-How about class of context-free languages?
Not unless you limit it further (e.g., \# of rules)


## Punchline

- But class of probabilistic context-free languages is learnable in the limit!!
- If Mom has to output sentences randomly with the appropriate probabilities,
- she's unable to be too evil
- there are then perfect Babies that are guaranteed to converge to an appropriate probabilistic CFG
- l.e., from hearing a finite number of sentences, Baby can correctly converge on a grammar that predicts an infinite number of sentences.
- Baby is generalizing! Just like real babies!


## Perfect fit to perfect, incomplete data



## Imperfect fit to noisy data



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## Imperfect fit to noisy data


$\pm$ Input Data
$-2 x^{\wedge} 2-6 x+6$

$-8 x^{\wedge} 6+72.8 x^{\wedge} 5-250^{*} x^{\wedge} 4+$
$401^{*} x^{\wedge} 3-297^{*} x^{\wedge} 2+79.2^{*} x+$
6

- More Input Data

Will an ungrammatical sentence ruin baby forever? (yes, under the conservative strategy ...)
Or can baby figure out which data to (partly) ignore?

## Imperfect fit to noisy data



$$
\begin{aligned}
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& 2 x^{\wedge} 2-6 x+6 \\
& -8 x^{\wedge} 6+72.8 x^{\wedge} 5-250^{*} x^{\wedge} 4+ \\
& 401^{*} x^{\wedge} 3-297^{*} x^{\wedge} 2+79.2^{*} x+ \\
& 6 \\
& - \text { More Input Data }
\end{aligned}
$$

Will an ungrammatical sentence ruin baby forever? (yes, under the conservative strategy ...)
Or can baby figure out which data to (partly) ignore? Statistics can help again ... how?

# Frequencies and Probabilities in Natural Languages 

Chris Manning and others

## Models for language

- Human languages are the prototypical example of a symbolic system
- From the beginning, logics and logical reasoning were invented for handling natural language understanding
- Logics and formal languages have a language-like form that draws from and meshes well with natural languages

- Where are the numbers?


## Dominant answer in linguistic theory：Nowhere

Chomsky again（1969：57；also 1956，1957，etc．）：
【＂It must be recognized that the notion＇probability of a sentence＇is an entirely useless one，under any known interpretation of this term．＂
【 Probabilistic models wrongly mix in world knowledge
I New York vs．Dayton，Ohio
【 They don＇t model grammaticality［also，Tesnière 1959］
I Colorless green ideas sleep furiously
I Furiously sleep ideas green colorless
I［But see Pereira 2005］

## Categorical linguistic

theories (GB, Minimalism, LFG, HPSG, CG, ...)

【Systems of variously rules, principles, and representations is used to describe an infinite set of grammatical sentences of the language
I Other sentences are deemed ungrammatical
【 Word strings are given a (hidden) structure


## The need for frequencies / probability distributions

The motivation comes from two sides:
I Categorical linguistic theories claim too much:
I They place a hard categorical boundary of grammaticality, where really there is a fuzzy edge, determined by many conflicting constraints and issues of conventionality vs. human creativity
【 Categorical linguistic theories explain too little:
I They say nothing at all about the soft constraints which explain how people choose to say things
I Something that language educators, computational NLP people and historical linguists and sociolinguists dealing with real language - usually want to know about

## 1. The hard constraints of categorical grammars

【 Sentences must satisfy all the rules of the grammar
I One group specifies the arguments that different verbs take - lexical subcategorization information
I Some verbs must take objects: *Kim devoured [ * means ungrammatical]
I Others do not: *Kim's lip quivered the straw
I Others take various forms of sentential complements
I In NLP systems, ungrammatical sentences don't parse
I But the problem with this model was noticed early on:
I "All grammars leak." (Sapir 1921: 38)

## Example: verbal clausal subcategorization frames

- Some verbs take various types of sentential complements, given as subcategorization frames: I regard: __ NP[acc] as \{NP, AdjP\} I consider: __ NP[acc] \{AdjP, NP, VP[inf]\} I think: __ CP[that]; __ NP[acc] NP
【 Problem: in context, language is used more flexibly than this model suggests
I Most such subcategorization 'facts' are wrong


## Standard subcategorization rules（Pollard and Sag 1994）

－We consider Kim to be an acceptable candidate
【 We consider Kim an acceptable candidate
I We consider Kim quite acceptable
I We consider Kim among the most acceptable candidates
－＊We consider Kim as an acceptable candidate
【 We consider Kim as quite acceptable
【 We consider Kim as among the most acceptable candidates
【 ？＊We consider Kim as being among the most acceptable candidates

# Subcategorization facts from The New York Times 

Consider as:
I The boys consider her as family and she participates in everything we do.
【 Greenspan said, "I don't consider it as something that gives me great concern.
【 "We consider that as part of the job," Keep said.
I Although the Raiders missed the playoffs for the second time in the past three seasons, he said he considers them as having championship potential.

- Culturally, the Croats consider themselves as belonging to the "civilized" West, ...


# More subcategorization facts: regard 

Pollard and Sag (1994):
【 *We regard Kim to be an acceptable candidate

- We regard Kim as an acceptable candidate

The New York Times:
【 As 70 to 80 percent of the cost of blood tests, like prescriptions, is paid for by the state, neither physicians nor patients regard expense to be a consideration.

- Conservatives argue that the Bible regards homosexuality to be a sin.


## More subcategorization facts: turn out and end up

Pollard and Sag (1994):

- Kim turned out political
- *Kim turned out doing all the work

The New York Times:

- But it turned out having a greater impact than any of us dreamed.

Pollard and Sag (1994):

- Kim ended up political
- *Kim ended up sent more and more leaflets

The New York Times:

- On the big night, Horatio ended up flattened on the ground like a fried egg with the yolk broken.


## Probability mass functions: subcategorization of regard



## Probability mass functions: subcategorization of regard



## Leakage leads to change

- People continually stretch the 'rules' of grammar to meet new communicative needs, to better align grammar and meaning, etc.
- As a result language slowly changes

I while: used to be only a noun (That takes a while); now mainly used as a subordinate clause introducer (While you were out)
I e-mail: started as a mass noun like mail (most junk email is annoying); it's moving to be a count noun (filling the role of e-letter): I just got an interesting email about that.

## Blurring of categories: "Marginal prepositions"

I An example of blurring in syntactic category during linguistic change is so-called 'marginal prepositions' in English, which are moving from being participles to prepositions
I Some still clearly maintain a verbal existence, like following, concerning, considering; for some it is marginal, like according, excepting; for others their verbal character is completely lost, such as during [cf. endure], pending, notwithstanding.

## Verb (VBG) $\Rightarrow$ Preposition IN

As verbal participle, understood subject agrees with noun:
【 They moved slowly, toward the main gate, following the wall

- Repeat the instructions following the asterisk

A temporal use with a controlling noun becomes common:
【 This continued most of the week following that ill-starred trip to church
Prep. uses (meaning is after, no controlling noun) appear

- He bled profusely following circumcision
- Following a telephone call, a little earlier, Winter had said


## Mapping the recent change of following: participle $\Rightarrow$ prep.

I Fowler (1926): "there is a continual change going on by which certain participles or adjectives acquire the character of prepositions or adverbs, no longer needing the prop of a noun to cling to ... [we see] a development caught in the act"
【 Fowler (1926) -- no mention of following in particular
I Fowler [Gowers] (1948): "Following is not a preposition. It is the participle of the verb follow and must have a noun to agree with"
I Fowler [Gowers] (1954): generally condemns temporal usage, but says it can be justified in certain circumstances

## 2. Explaining more: <br> What do people say?

- What people do say has two parts: I Contingent facts about the world

I People in Minnesota have talked a lot about snow falling, not stocks falling, lately
I The way speakers choose to express ideas using the resources of their language
I People don't often put that-clauses pre-verbally:

- That we will have to revise this program is almost certain
- The latter is properly part of people's Knowledge of Language-i.e., part of linguistics.


## What do people say?

【 Simply delimiting a set of grammatical sentences provides only a very weak description of a language, and of the ways people choose to express ideas in it

- Probability densities over sentences and sentence structures can give a much richer view of language structure and use
I In particular, we find that the same soft generalizations and tendencies of one language often appear as (apparently) categorical constraints in other languages
【 A syntactic theory should be able to uniformly capture these constraints, rather than only recognizing them when they are categorical


## Example: Bresnan, Dingare

## \& Manning

【 Project modeling English diathesis alternations (active/passive, locative inversion, etc.)

- In some languages passives are categorically restricted by person considerations:
I In Lummi (Salishan, Washington state), $1 / 2$ person must be the subject if other argument is 3rd person. There is variation if both arguments are 3rd person. (Jelinek and Demers 1983) [cf. also Navajo, etc.]
I *That example was provided by me
I *He likes me
I $\sqrt{ }$ am liked by him


## Bresnan, Dingare \&

## Manning

- In English, there is no such categorical constraint, but we can still see it at work as a soft constraint.
- Collected data from verbs with an agent and patient argument (canonical transitives) from treebanked portions of the Switchboard corpus of conversational American English, analyzing for person and act/pass

|  | Active | Passive |
| :--- | ---: | ---: |
| $1 / 2 \mathrm{Ag}, 1 / 2 \mathrm{Pt}$ | 158 | $0(0.0 \%)$ |
| $1 / 2 \mathrm{Ag}, 3 \mathrm{Pt}$ | 5120 | $1(0.0 \%)$ |
| $3 \mathrm{Ag}, 1 / 2 \mathrm{Pt}$ | 552 | $16(2.8 \%)$ |
| $3 \mathrm{Ag}, 3 \mathrm{Pt}$ | 3307 | $46(1.4 \%)$ |

## Bresnan, Dingare \&

## Manning

I While person is only a small part of the picture in determining the choice of active/passive in English (information structure, genre, etc. is more important), there is nonetheless a highly significant ( $\mathrm{X}^{2} \mathrm{p}<0.0001$ ) effect of person on active/passive choice

- The exact same hard constraint of Lummi appears as a soft constraint in English
IThis behavior is predicted by the universal hierarchies within a stochastic OT model (which extends existing OT approaches to valence - Aissen 1999, Lødrup 1999)
I Conversely linguistic model predicts that no "antiEnglish" [which is just the opposite] exists


## Conclusions

-There are many phenomena in language that cry out for non-categorical and probabilistic modeling and explanation

- Probabilistic models can be applied on top of one's favorite sophisticated linguistic representations!
I Frequency evidence can enrich linguistic theory by revealing soft constraints at work in language use

