

CS3000: Algorithms & Data — Summer 2025 — Laney Strange

APP 3

Due: May 15th, 2025 @ 11:30am via [Gradescope](#)

Name:

- APPs will be assigned towards the end of roughly two lectures each week. You'll put together a solution to a short problem that we'll all use in the following lecture. We'll have time set aside to do these in class, or you can work on your own.
- You may handwrite your solutions, or typeset them in $\text{\LaTeX}$ or another system.
- APPs will be graded on completeness. They must be submitted by 11:30am (just before lecture) on the due date. They will not be accepted late, but we drop 3 of them (out of 8 total).
- Collaboration is strongly encouraged for APPs!

Problem 1.

Below is the pseudocode for Quicksort. Complete the proof we started in class to show the correctness of PARTITION. In particular, use a loop invariant to show that, at the beginning of each iteration of the loop at lines 3-6, for any array index k , if $i + 1 \leq k \leq j - 1$ then $A[k] > x$.

QUICKSORT(A, p, r)

```
1  if  $p < r$ 
2       $q = \text{PARTITION}(A, p, r)$ 
3      QUICKSORT( $A, p, q - 1$ )
4      QUICKSORT( $A, q + 1, r$ )
```

PARTITION(A, p, r)

```
1   $x = A[r]$ 
2   $i = p - 1$ 
3  for  $j = p$  to  $r - 1$ 
4      if  $A[j] \leq x$ 
5           $i = i + 1$ 
6          swap  $A[i], A[j]$ 
7  swap  $A[i + 1], A[r]$ 
8  return  $i + 1$ 
```

Solution: