

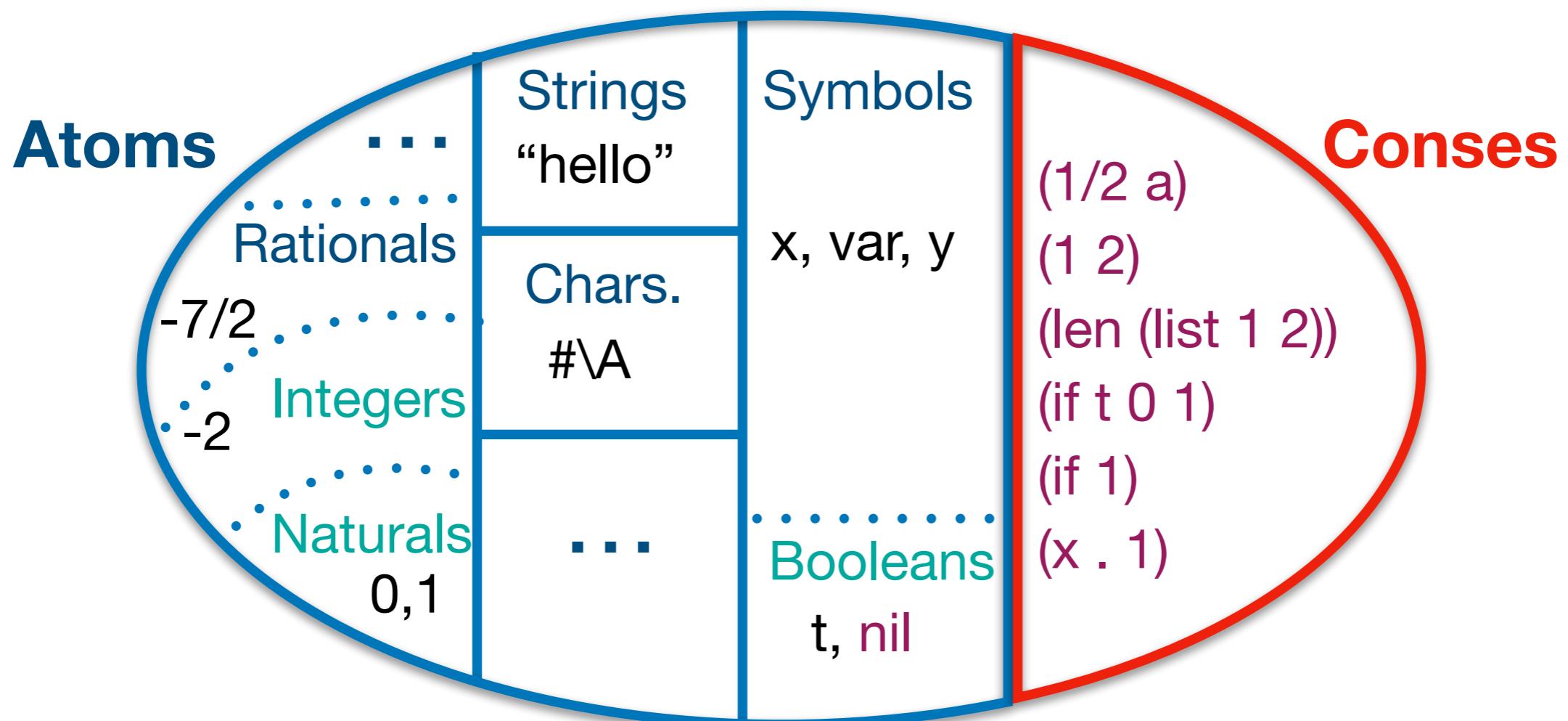
# The ACL2s Language

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# Objectives

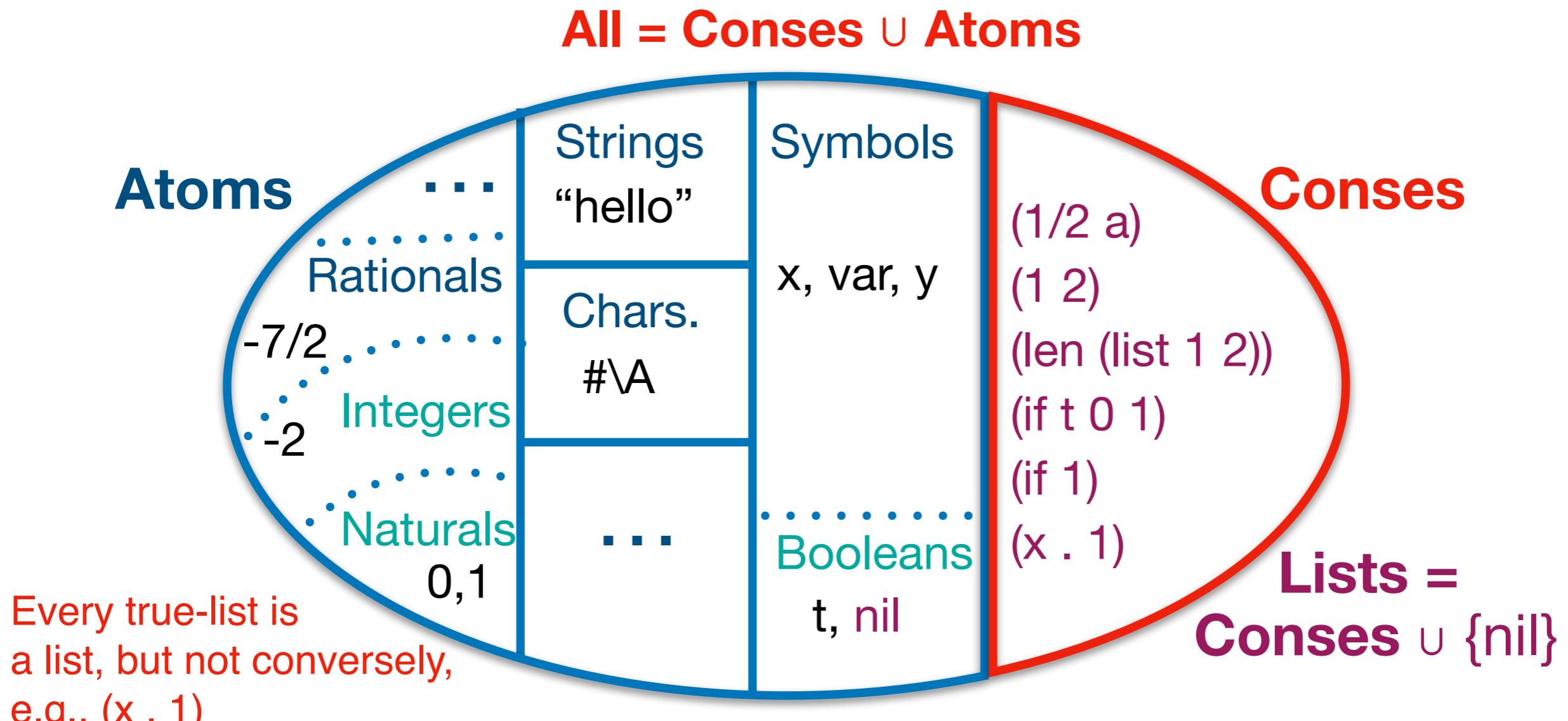
- ▶ Lists
- ▶ Contract violations
- ▶ Termination
- ▶ ACL2s Demo

# Expressions



Expressions are elements of the universe, but not conversely  
Which conses are expressions?

# ACL2 Universe: Conses

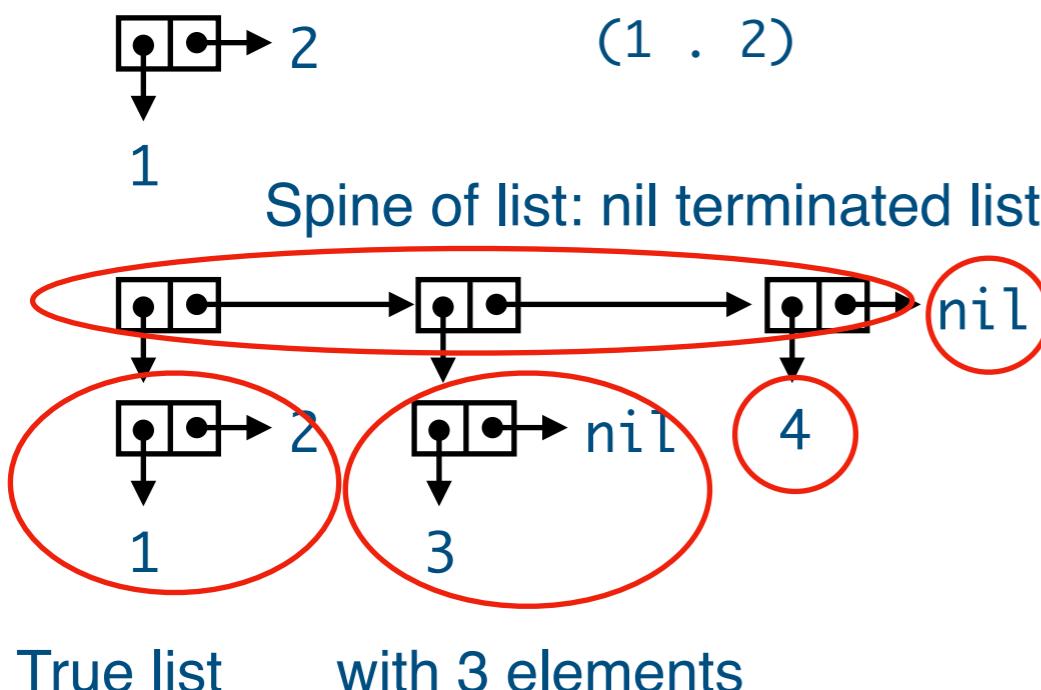


# True-Lists = $\cup_{i \in \mathbb{N}} TL_i$

$$TL_0 = \{ () \}, TL_{i+1} = TL_i \cup \{(\text{cons } x \ l) : x \in All, l \in TL_i\}$$

# Conses, Dotted Pair Notation

- ▶ Built-in functions & signatures
  - ▶ consp: All  $\rightarrow$  Boolean
  - ▶ cons: All  $\times$  All  $\rightarrow$  Cons
  - ▶ car: List  $\rightarrow$  All
  - ▶ cdr: List  $\rightarrow$  All



- ▶ A cons is just a pair, eg,  $(\text{cons } 1 \ 2)$
- ▶ Since pairs are nested, conses are trees, eg,  $(\text{cons } (\text{cons } 1 \ 2) \ (\text{cons } (\text{cons } 3 \ \text{nil}) \ (\text{cons } 4 \ \text{nil})))$
- ▶ Dotted pair notation simplification rules
  - ▶  $(x . \text{nil}) \rightarrow (x)$
  - ▶  $(\dots . (x \dots)) \rightarrow (\dots x \dots)$

$((1 . 2) . ((3 . \text{nil}) . (\text{4} . \text{nil})))$   
 $((1 . 2) . ((3) . (4)))$   
 $((1 . 2) (3) . (4))$   
 $((1 . 2) (3) 4)$

# Conses

## ▶ Built-in functions & signatures

- ▶ `consp`: All  $\rightarrow$  Boolean
- ▶ `cons`: All  $\times$  All  $\rightarrow$  Cons
- ▶ `car`: List  $\rightarrow$  All
- ▶ `cdr`: List  $\rightarrow$  All

▶  $\llbracket (\text{cons } x \ y) \rrbracket = (\llbracket x \rrbracket . \llbracket y \rrbracket)$

▶  $\llbracket (\text{consp } x) \rrbracket = t$  iff  $\llbracket x \rrbracket$  is of the form (...) but is not ()

▶  $\llbracket (\text{car } x) \rrbracket = a$ , when  $\llbracket x \rrbracket = (a \ . \ b)$ , nil otherwise

▶  $\llbracket (\text{cdr } x) \rrbracket = b$ , when  $\llbracket x \rrbracket = (a \ . \ b)$ , nil otherwise

## ▶ Examples

- ▶  $\llbracket (\text{consp nil}) \rrbracket = \text{nil}$  (since  $\text{nil} = ()$ )
- ▶  $\llbracket (\text{car } ()) \rrbracket = \text{nil}$ ,  $\llbracket (\text{cdr } ()) \rrbracket = \text{nil}$  (since  $\text{nil}$  is a List)
- ▶  $\llbracket (\text{consp } (\text{cons } \text{nil} \ \text{nil})) \rrbracket = t$  (since  $\llbracket (\text{cons } \text{nil} \ \text{nil}) \rrbracket = (\text{nil} \ . \ \text{nil})$ )
- ▶  $\llbracket (\text{car } (\text{cdr } (\text{cons } (\text{if } t \ 3 \ 4) \ (\text{cons } 1 \ ())))) \rrbracket = 1$

```
(definec true-listp (l :all) :bool
  (if (consp l)
      (true-listp (rest l))
      (equal l ())))
```

# Macros

- ▶ List construction is prevalent, so ACL2s provides `list`
- ▶  $(\text{list } x_1 \ x_2 \ \dots \ x_n)$  abbreviates (or is shorthand for)  
 $(\text{cons } x_1 \ (\text{cons } x_2 \ \dots \ (\text{cons } x_n \ \text{nil}) \ \dots))$
- ▶ Notice that `list` takes an arbitrary number of arguments
  - ▶  $\llbracket (\text{list}) \rrbracket = ()$
  - ▶  $\llbracket (\text{list } 1) \rrbracket = (1 \ . \ \text{nil}) = (1)$
  - ▶  $\llbracket (\text{list } 1 \ 2) \rrbracket = (1 \ . \ (2 \ . \ \text{nil})) = (1 \ 2)$
- ▶ `list` is a macro: it gets expanded into an expression
- ▶ `first`, `rest` abbreviate `car`, `cdr`
- ▶ `caar`, `cadr`, `cdar`, ..., abbreviate  $(\text{car } (\text{car } \dots))$ ,  $(\text{car } (\text{cdr } \dots))$ , ...
- ▶ `second`, `third`, ..., equivalent to `cadr`, `caddr`, ...

# Cond

- ▶ `(cond (c1 e1)  
          (c2 e2)  
          ...  
          (cn en))`

expands into

```
(if c1  
    e1  
    (if c2  
        e2  
        ...  
        (if cn  
            en  
            nil)))
```

- ▶ We will always use `t` for the last test in a `cond` (so the `nil` will not be reachable)

# ACL2s Demo

- ▶ ACL2s perspective
- ▶ Creating a project, syncing files, refresh
- ▶ Loading hwk1
- ▶ Split window
- ▶ ACL2s mode
- ▶ REPL
- ▶ Atoms
- ▶ Definitions
- ▶ Line
- ▶ GUI interface
- ▶ Termination
- ▶ Contracts