CS1800 Day 5

Admin:

- HW1 due today (number representation)
 - did you format it properly?
- HW2 released today (logic)

Content:

- conditionals
 - contrapositive, inverse, converse
 - bi-conditionals
- quantifiers (universal & existential)
 - negating each
 - combining them
 - "for every x there exists a y"
 - "there exists a y for every x"

BOOLEAN OPERATORS A WALK DOWN MEMORY LANE: (DISSUNCTIVE) (CONSUNCTIVE) NOT XVX YVX TRUE ONLY WHEN SWAPS TRUE ONCH WHEN TRUTH ANY INPUT TRUE ALL INPUTS TRUE VALUE

WALK DOWN MEMORY LANE: QUANTIFIER FOR ALL $\forall x \text{ Loves - CS 1800(x)}$ $\exists x \text{ Loves - CS 1800(x)}$ "EVERY STUDENT X LOVES" (THERE IS A STUDENT X IT A WALK DOWN MEMORY LANE: CONDITIONALS

IF X THEN Y

X	Υ	$X \rightarrow Y$
F	F	COUNTER - EXAMPLES
F	Т	- X IS TRUE BUT Y ISN'T
Т	F	T - SUDNS X-Y 15 FALSE
Т	Т	7

USEFUL FACT

QUILK EXAMPLE

	C	Com	LETE	
X-0 Y 15 TONE 7X=T-07	X= T	Tru	TABLE X=F	
EVERYWHERE EXCEPT Y=F			•	
COUNTER EXAMPLE	X	Υ	TX - (Y)	
	F	F	F	
XATY	F	Τ	T	
	Т	F	T	
	Т	Т	T	

IN CLASS ACTIVITY

Given the following statements:

G = life you gives you lemons

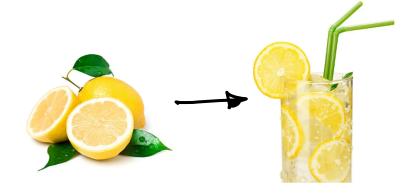
M = you make lemonade

For each statement below:

- express it using logic symbols
- create a truth table for the statement (for every combination of G, M, is it true?)
- identify which of the four statements below are logically equivilent to other statements given

Statements:

- If life gives you lemons, then you make lemonade
- If you are not making lemonade, life hasn't given you lemons
- If you make lemonade, then life has given you lemons
- If you haven't been given lemons, then you aren't making lemonade



6	\sim	G ->	w	76 -> 7 M
£	F			
t	T			
T	F			
T	7			
		\		•

SOMETHING LIKE THIS

SOMETHING LIKE THIS?

ACTIVITY ANSWERS FOCLOW

(NO PEEKING!)

			1F	Guen	LEM	not n	ake ade	MAKE	A0E	NoT	GwEN	CEM
1	1		THEN	MAKE	ROE	NOT G	ien rem	Given	LEM	NOT	MAK	E ADE
79	7 M	6 纂	W.	6	· W	- M-	→ 76	1 2 +	6	76	→ -	2 M
R	T	F	F	T		て		۲			T	
T	(F)	F	T	T		T		7			F	
7	IX	T	F	F		F		T			T	
F	(F) T	T	+		T		+			T	
	. To	KEN WE LAVE		6=T M=F	-	7M=7 76=	_	M=	`		0=7 1=F	

	1F	6,464	LEM	NOT	make a	DE	MA	KE A	30	NoT	Gwer	م رجس
THEN		make ace		NOT GIVEN LEM		GIVEN LEM		NOT	MA	KE ADE		
G 💥	W.	G →	M	- N	\ -> 7(S	1 4	-	6	70	G →	7M
F	F	T			7			T			T	
F	T	7			T			F			F	
Т	F	F			F			T			T	
Т	T	T			T			Ţ			T	
	•	7	ALLY	7			1	,	•	7		

EDUNIENT &

FOUNTENT

Cousins	of G → M:	original statement	contrapositive	converse	inverse
G 💥	W.	G + N	7M ->76	MAG	76 - 7M
F	F	T	T	T	T
F	T	て	て	F	F
Т	F	F	F	て	T
T	T	7	T	T	T

Takeaways:

- a statement and its contrapositive are logically equivilent (tip: it may be easier to work with one or other, use the simpler the one)
- a statement is not logically equivilent to converse or inverse

"If life gives you lemons, then you make lemonade" does not imply that because you're making lemonade, you must have been given lemons

B F. FT TF TT

QUICK NOTATION: BALKWARDS CONDITIONAL

X4-Y IS SAME AS Y-X

Bi-con	ditional	: X ←→ Y	$= (X \to Y) \land (X \leftarrow Y)$	1	IF AND	0NLY 1F
			original	converse	bi-conditional	"1FF"
·	X	Υ	X → Y	∀→ X	X I	
•	F	F	T	T	τ	
•	F	Т	T	F	E	
•	Т	F	F	T	F	
•	Т	Т	T		T	

If $X \leftrightarrow Y$ is True then either:

- X=Y=0
- X=Y=1

Either way, x and y are always the same. Bi-conditionals express logical equivilence

LOOTIUTAI Y + X - X AND Y HAVE SAME TRUTH VALUE: - WHEN ONE IS TRUE, SO IS OTHER NHEN ONE IS FAISE, SO IS OTHER

Another notation for biconditionals: iff = "if and only if" ex: I'll wear a rainjacket if and only if its raining

New topic:
Quantifiers (negating & combining them)

Negating Quantifiers: - عاد در د ۲

Statement 1:

Some student, in class, has a birthday today!

Negation of statement 1:

For all students x, it is not their birthday today

Statement 2:

Every student in the class loves chocolate

Negation of statement 2: there exists a student in the class who doesn't love chocolate

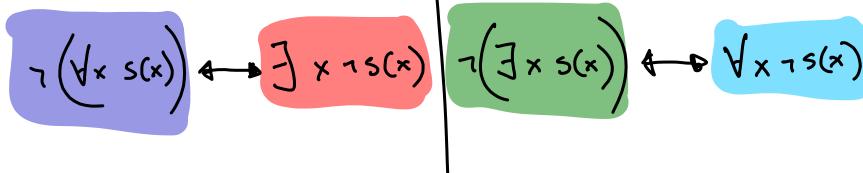
Logic

STUDENT

X'S BIRTHDAY

Negating Quantifiers

Iff a statement isn't true for all x, then there is an x for which it isn't true



Iff there is no x for which a statement is true, then x is not true for all x



5, MULTANEOUS ROCK-PAPER-SCISSORS

COMBINING QUANTIFIERS: FOR ALL X, THERE EXISTS Y WIN(XIY) = X BEAT Y @ ROCK PAPER SCHEME XIY STUDENTS FOR EVERY STUDENT X, THERE IS ANOTHER STUDENT Y WHO THEY'VE BEATEN (YIX) WIN YEX W TRUE, EVERY BODY X BEAT SOMEBODY ELSE Y EACH X MAY PICK ITS ONN Y

PREVIOUSLY FOR ALL X, THERE EXISTS Y X Y Y E

THERE Exists y FOR ALL X COMBINING QUANTIFIERS: WIN(XIY) = X BEAT Y @ ROCK PAPER SCHEME XIY STUDENTS THERE IS A STUDENT Y, WHO GR EVERY STUDENTX A Y HAS BEATEN X 3 y y x min(xix) CAUSE FALSE, ONE STUDENT DIDN'T BEAT EVERYONE ELSE EVERY X IS SATISFIED BY SAMEY

FOR ALL X, THERE EXISTS Y THERE EXISTS Y FOR ALL X X Y VE BY SAME Y ONN Y

In Class Activity

For each sentence immediately below:

- express it using logical symbols
- express its negation using logical symbols
- translate that negation back to english
- There is a good discrete structure textbook
- Everybody loves ice cream

For each sentence immediately below:

- express it using logical symbols
- Everyone has somebody who can make them smile
- There is someone who ran the race faster than anybody else

7 7 x Como(r) VX76000(x) A coop TEXT 1 /x ICL(x) x = Person Jx 71CL(x) (CL(x)=

XIY ARE PEOPLE Everyone has somebody who can make them smile Yx Jy SMILE (YX) GMILE (YIX) = PERSON X SMILE WINS(YX) \ NINS(YX) \ NINS(YX) \ NINS(YX) \ NINS(YX) \ NINS(YX) \ X14 RODNERS

Y RAN FASTER THAN