CS1800 Day 5

#### Admin:

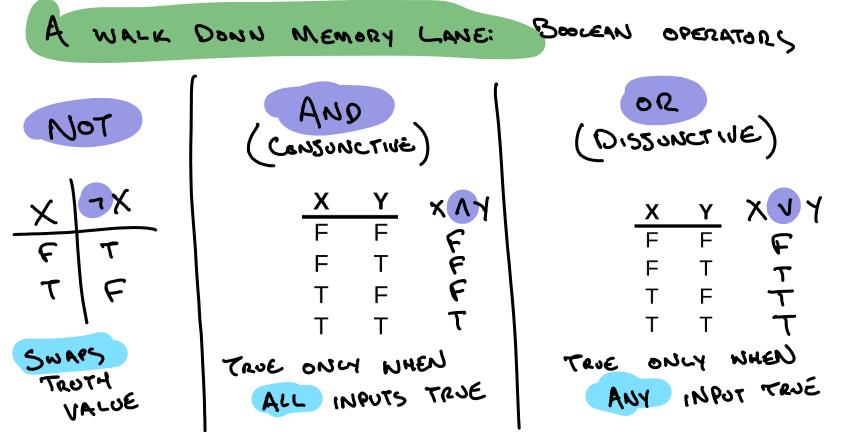
- HW1 due today (number representation)
  - did you format it properly?
- HW2 released today (logic)

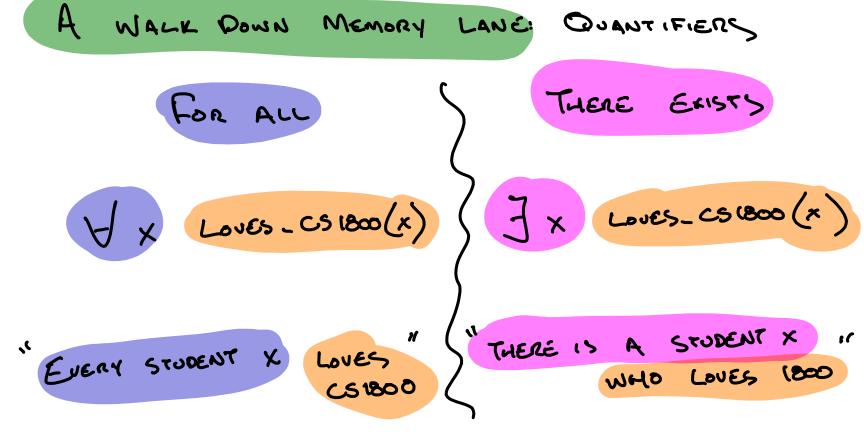
## Content:

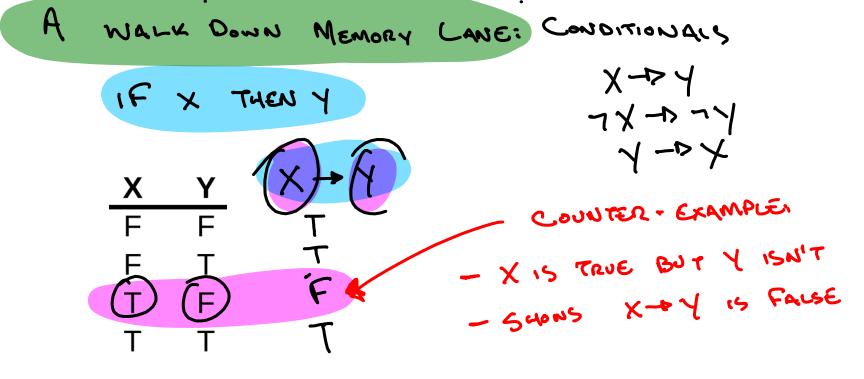
- conditionals

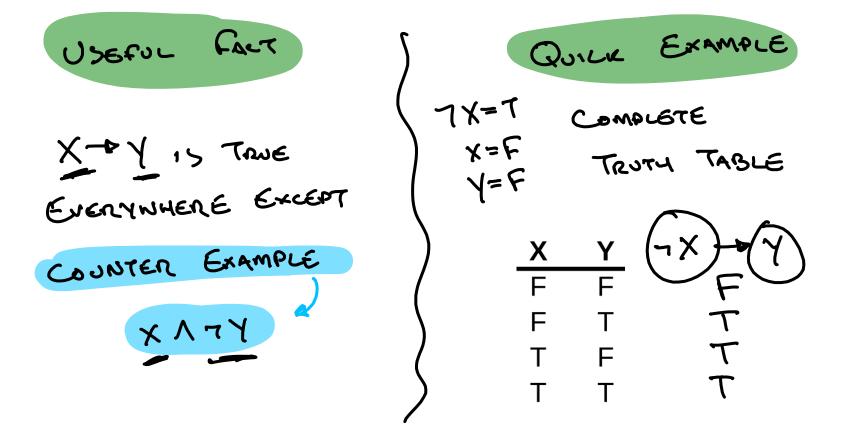
- contrapositive, inverse, converse
- bi-conditionals
- quantifiers (universal & existential)
  - negating each
  - combining them
    - "for every x there exists a y"
    - "there exists a y for every x"

(1234+17)08 = 1354.8 + 17.8









# IN CLASS ACTIVITY

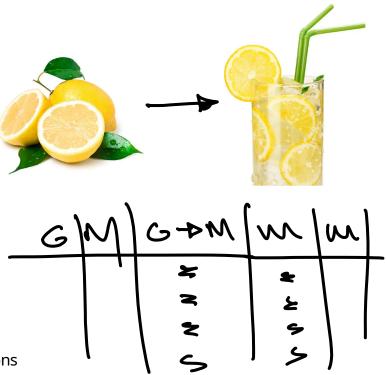
Given the following statements: G = life you gives you lemons M = you make lemonade

For each statement below:

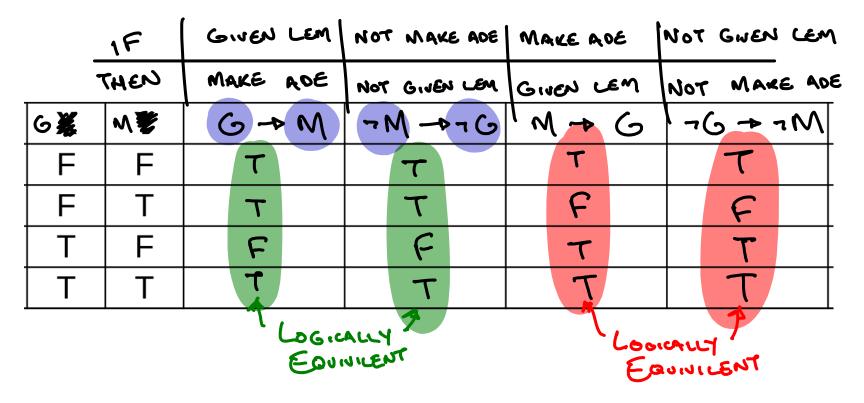
- express it using logic symbols
- create a truth table for the statement
  - (for every combination of G, M, is it true?)
- identify which of the four statements below are logically equivilent to other statements given

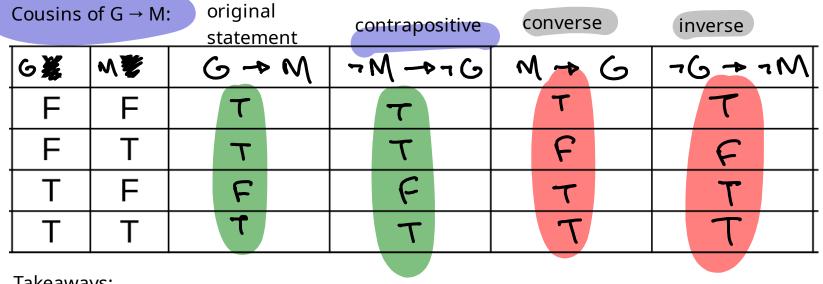
### Statements:

- If life gives you lemons, then you make lemonade
- If you are not making lemonade, life hasn't given you lemons
- If you make lemonade, then life has given you lemons
- If you haven't been given lemons, then you aren't making lemonade



			1F	GIVEN LEM	NOT MAKE ADE	MAKE ADE	NOT GWEN LEM
•			Then	Make Ade	NOT GIVEN LEM	Given LEM	NOT MARE ADE
ч6 Г	21	G¥€	₩	G→M	- M - + - G	M + G	76 → 7M
$\overline{\mathbf{T}}$	T	F	F	Т	Т	T	Т
$\mathbf{\overline{D}}$	F	F	Т	Т	Т	F	F
F	Ī	Т	F	F	F	T	$\top$
F	(F)	) Т	Т	1	Т	Т	T
ا می ب	UNT LAR	El		G=T M=F	7M=T 7G=F	M=T G=F	76=T 7M≠F





Takeaways:

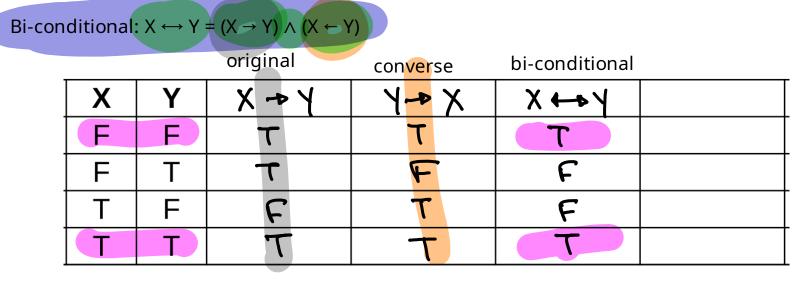
- a statement and its contrapositive are logically equivilent

(tip: it may be easier to work with one or other, use the simpler the one)

- a statement is not logically equivilent to converse or inverse
 "If life gives you lemons, then you make lemonade" does not imply that because you're making lemonade, you must have been given lemons

# QUICK NOTATION: BALKWARDS CONDITION

# XANY IS SAME AS Y-X



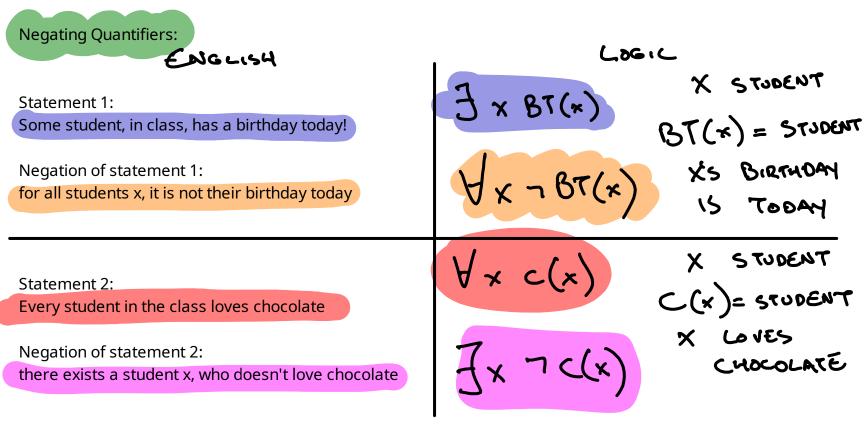
If  $X \leftrightarrow Y$  is True then either:

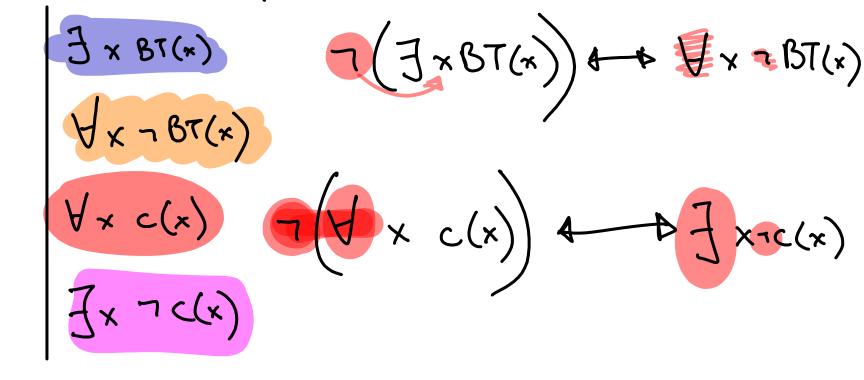
- X=Y=0
- X=Y=1

Either way, x and y are always the same. Bi-conditionals express logical equivilence

Another notation for biconditionals: iff = "if and only if" ex: I'll wear a rainjacket if and only if its raining New topic:

Quantifiers (negating & combining them)

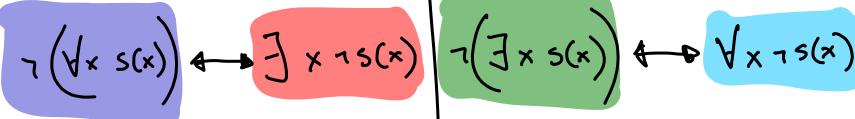




Negating Quantifiers

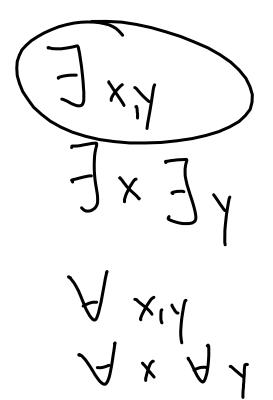
Iff a statement isn't true for all x, then there is an x for which it isn't true

Iff there is no x for which a statement is true, then x is not true for all x



.

YJX Ţx



#### In Class Activity

For each sentence immediately below:

- express it using logical symbols
- express its negation using logical symbols
- translate that negation back to english
- There is a good discrete structure textbookEverybody loves ice cream

For each sentence immediately below: - express it using logical symbols

- Everyone has somebody who can make them smile
- There is someone who ran the race faster than anybody else

There is a good discrete structure textbook 
$$\chi = B \infty \mathcal{L}$$
  
 $DST(x) = Trive iF$   
 $T(J \times DST(x)) \longrightarrow J \times TDST(x)$   
For all books they are not good discrete structures textbooks  $Text Book$   
 $Everybody loves ice cream$   
 $\chi = Person$   
 $Lic(x) = Person \chi$   
 $Lic(x) = Person \chi$   
 $Loves ice$ 

X y= PERSON - Everyone has somebody who can make them smile Smile(y,x)= YXJY SMILE(Y,X) TRUE ,F PERSONY MAKES PERSON X SMILE - There is someone who ran the race faster than anybody else XIY = RACENS Wind (XX) Tx Vy Win(x,y)= True if x RAN FASTER THAN Y